Lateral Loading of a Rigid Rock Socket Embedded in a Damage-Sysceptible Poroelastic Solid



Abstract: The paper presents a computational assessment of the inßuence of damage on the behavior of a rigid rock socket embedded in a ßuid-saturated poroelastic solid. The iterative computational scheme takes into consideration the irreversible alteration in the ßuid-saturated poroelastic solid.

embedded at the surface of a damage-susceptible poroelastic halfspace. In addition to the consideration of the alteration in the elasticity and hydraulic conductivity characteristics with strain, we also consider the inßuence of the stress-state dependency on the evolution of damage. In this latter approach, the isotropic damage evolution depends on the serteesile/compressiveof the Þrst invariant of the effective stress tensor. Such an approximation is in keeping with common experimental observations conducted on soft rocks that damage cannot be initiated through an increase in the compressive effective conbning stress that can be applied to a geomaterial. This assumption is in agreement with the experimental observations in the geological porous media with an interconnected network of pores including soft rocks and subjected to stress levels well below the failure. The studies by Katti and Desai 1995 and Park and Desai 2000, that use the disturbed state concepts indicate that intergranular bonded materials including overconsolidated clays and saturated sands with potential for exhibiting microstructural instability in the form of liquefaction, when subjected to high stress levels, can experience damage even at stress states that are compressive. The specibo problem examined in the paper is illustrated in Fig. 1. The surface of the damage susceptible poroelastic medium is assumed to be free draining. The interface between the rigid rock socket and the poroelastic medium can possess pore pressure boundary conditions that correspond to either fully drained or impervious conditions. The displacements of the poroelastic medium are continuous across the rock socketDgeomaterial interface. The dominant displacement of the embedded rock socket corresponds to lateral displacement at the point of application of the load . This load is represented by a time dependency in the form of a Heaviside step function. The time-dependent consolidation response of the rock socket is assessed in relation to its displacement at the point of application of Pt.

Go erning Eq_ations

The basic investigation associated with this paper relates to the incorporation of damage mechanics within the context of the classical theory of poroelasticity proposed by Bidt941. The evolution of stress-state-dependent isotropic damage will inßuence the alteration of the basic material parameters associated with the poroelastic model, in terms of the elastic modulus and the hydrau-

sponds to rupture and irreversible deformations within the porous skeleton. In the limit when DD_C, the material response is bound to deviate from the elastic model that is adopted in the current study. It is therefore desirable to limit the range of applicability of the damage to a critical value, which can be used as a normalizing parameter, against which levels of damage can be compared. In a geomaterial that experiences isotropic damage, the net stress tensor is related to the stress tensor in the undamaged state by

$$_{ij}^{n} = \frac{_{ij}}{1 \cdot D}$$

The deformability parameters applicable to an initially isotropic elastic material, which experiences isotropic damage, can be updated by adjusting the linear elastic shear modulus by its equivalent applicable to the damaged state, i.e.

In the following, we examine the mechanics of poroelastic materials that exhibit isotropic damage through the introduction of a poroelastic model with a constitutive relationship of the form

$$_{ij} = 2 \cdot 1 \cdot D$$
 $_{ij} + \frac{2 \cdot 1 \cdot D}{1 \cdot 2}$ $_{kk \ ij} + p_{\ ij}$ 4

where $_{ii} = u_{i,i} + u_{i,i} / 2 = infinitesimal$ strain tensor; $_{kk} = u_{i,i}$; =linear elastic shear modulus; =PoissonÕs ratio; and ii = KroneckerÖs delta function. Implicit in Eq. is the assumption that PoissonOs ratio for the material experiencing damage ishanges in the permeability in the localization zones. unaltered from its value applicable to the undamaged material. This assumption was put forward by Lemait 1984 in the strain equivalence hypothesis. In addition to the constitutive behavior draulic conductivity of sandstone due to the applied shear strains, debned by Eq. 4, it is also necessary to prescribe a damage Mahyari and Selvadurai 1998 have obtained the following relaevolution criterion that can be based on either micromechanical tionship for the dependency of hydraulic conductivity on the considerations or determined through experimentation. Experi-equivalent shear strain, which takes the form mental data on measurement of damage evolution are scarce; the limited data on sandstone were examined and they propose a damage evolution criterion that is debned by

$$\frac{D}{d} = \frac{d}{1+d} \cdot 1 \cdot \frac{D}{D_C}$$

where d=equivalent, shear strain debned by

$$_{d} = e_{ij}e_{ij}^{1/2}, \quad e_{ij} = {}_{ij} \cdot {}_{3kk}^{1} = {}_{ij}$$

and , =positive material constants. In this formulation, the normalizing damage measure is the critical damage which is associated with the damage corresponding to a limit value of the strength of the soft rock under uniaxial compression such that the deformations cannot be treated as a reversible elastic response and should be modeled by appeal to plasticity. It should be noted that the damage evolution function debned by Eqsatisbes the second law of thermodynamics. The evolution of the damage variable can be obtained by the integration of Eq. between limits D_0 and D, where D_0 is the initial value of the damage variable corresponding to the intact stateg., zero for materials in a virgin state. Integrating Eq. 5 between the limits, the evolution of D can be prescribed as follows:

$$D = D_{C} \cdot D_{C} \cdot D_{0} + d^{-D_{C}} \cdot a \exp d^{-D_{C}}$$

The development of damage criteria that can account for alterations in the hydraulic conductivity during evolution of damage in saturated geomaterials, is necessary for the modeling of such phenomena in poroelastic media. Literature on the coupling between

microcrack developments and permeability evolution in saturated geomaterials is primarily restricted to the experimental evaluation of the alteration in permeability of geomaterials that are subjected to triaxial stress states. Zoback and Byerlee75 have documented results of experiments conducted on granite and Shiping et al. 1994 give similar results for tests conducted on sandstone Fig. 2. These studies illustrate that the ßuid transport characteristics of geomaterials can be increased due to evolution of damage in porous fabric. Kiyama et all 996 observed similar results for the permeability evolution in granites subjected to triaxial stress states, which suggests that localization phenomena and Buid pressure-induced microfracturing could result in signibcant

Based on the experimental studies conducted by Shiping et al. 1994, which examine the damage-induced increase in the hv-

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niques for the study of the poroelasticity is now well established and details of these advances can be found in the references cited above. The basic Galerkin procedure can be applied to convert the governing partial differential equations to their matrix equivalents applicable to a Þnite domain. The resulting matrix equations take the form

K C u98.099 665.4019 Tm (T)Tj /F5 1 otin T otin T

block. In the Þnite element modeling, the interface between the rock socket and the poroelastic region does not correspond to a precise cylindrical surface; the mesh division adopted ensures that

Table 1. Comparison of Translational Stiffness of Rigid Rock Socket Subjected to Lateral Load and Elastic Behavior of Medium

	2P ₀ / d _h		
Method of analysis	L/d=1.0	L/d=2.0	L/d=4.0
Present study	6.28	9.71	11.26
Selvadurai and Rajapaks	7.03	9.8	11.44

- teration in the hydraulic conductivity characteristics;
- Poroelastic response with both damage evolution and hydraulic conductivity alteration; and
- Stress-state dependency of poroelastic response with both, damage evolution and hydraulic conductivity alteration.

Nymerical Resylts and Discyssion

The idealized problem corresponds to a rigid rock socket that is embedded at the surface of a half space. In the computational modeling, however, the domain is restricted to a Pnite region. Therefore it is necessary to evaluate the accuracy of the both the elasticity, and the hydraulic conductivity characteristics. domain used in the computational modeling in representing, ap-The porous skeletal material has a PoissonÕs ratioaonfd the proximately, a half-space region. To aid this evaluation we Þrst examine the problem of a rigid rock socket that is embedded in an ment of the problem is given by Selvadurai and Rajapalk965. The results obtained by Selvadurai and Rajapakse5 for the rigid rock socket were compared with equivalent results obtained through a Pnite element modeling of the domain of Pnite extent. The results obtained, through the two schemes, 10g/2d h, where P₀ is the lateral load; is the linear elastic shear modulus; d is the rock socket diameter; and is translational displacement of the head of the rock socket along the lateral load direction show reasonable agreement between the analytical and the computational estimates.

The computational modeling of a rigid rock socketig. 1 embedded in brittle poroelastic medium susceptible to damage length to diameterL/d ratios of the rigid rock socket. The nonwas conducted through the iterative Pnite element technique, the dimensional parameter, which is used to represent the transient computational algorithm of which is shown in Fig. 3, with basic

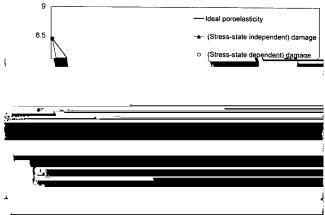


Fig. 7. Numerical results for transient translational displacement of rigid rock socket L/d=1.0 embedded in brittle poroelastic half space pervious interface

procedures that take into account damaged-induced alterations in pore ßuid is assumed to be nearly incompressible, i.e., elastic half-space region. This problem has been examined by a below the levels of damage corresponding the strain levels at the _u=0.499. We also assume that the damage evolution is well number of investigators and a comprehensive mathematical treat peak stress state. This excludes the necessity for consideration of any strain-softening effect. The theoretical basis of the computational scheme is therefore applicable to elastic states prior to the attainment of the peak stresteading to failure or the development of strain softeningpostpeak The material parameters used in the computations are those that are provided for sandstone by Shiping et al. 1994 and are as follows: E=8,300 MPa; =0.195; = =130 damage parameters _C compressive strength=30 MPa; T tensile strength=3 MPa; D_C=0.75 criti-

> The Pnite element discretization of the three-dimensional domain containing the laterally loaded rigid rock socket is shown in Fig. 6. The computational modeling is performed for different

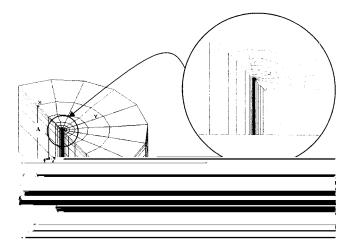


Fig. 6. Finite element discretization for rigid rock socket embedded in poroelastic half-space

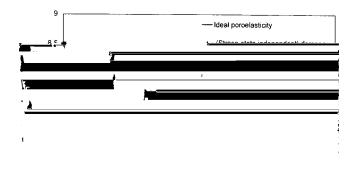
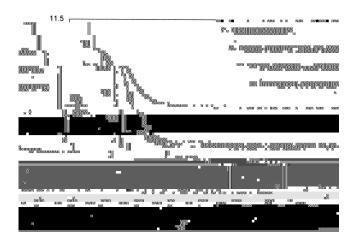


Fig. 8. Numerical results for transient translational displacement of rigid rock socket L/d=1.0 embedded in brittle poroelastic half space impervious interface





 $\label{eq:Fig. 13.} \textbf{Proposition Fig. 13.} \ \textbf{Numerical results for transient translational displacement of rigid rock socket $L/d=2.0$ embedded in brittle poroelastic half}$

L/d=2.0 and 4.0.

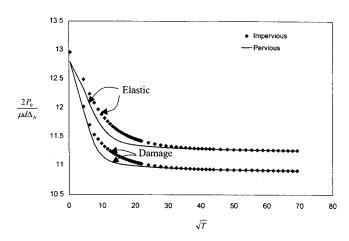


Fig. 19. Comparison of results for rigid rock socket with L/d=4.0 with either pervious or impervious interface between rock socket and poroelastic half space

interface and an impervious interface for the rock socket geom- **Concl**-**ding Remarks** etry, L/d=1.0. The inßuence of damage-induced alterations in the

case of the impervious interface is greater, but the overall changeThe classical theory of poroelasticity for a ßuid saturated brittle is not signiPcant. This is due to the highly localized response geomaterial has been adopted to investigate the isotropic damagebetween rock socket and poroelastic medium, which extends to ainduced alterations in both deformability and hydraulic conducregion substantially smaller in comparison to the surrounding po-tivity parameters. An iterative Pnite element technique has been roelastic medium. As a result any changes in the pore pressureused to examine the inßuence of the isotropic damage-induced variations at the interface region have negligible effects in com- alterations in the hydraulic conductivity of the porous medium on parison to variations in the bulk of the poroelastic medium. The the time-dependent response of a rigid rock socket, with different change can be attributed to slower rate of dissipation for the caselength to diameter ratios, embedded in a brittle poroelastic half of an impervious interface and any alteration in hydraulic conduc- space and subjected to a lateral load. Investigations have been tivity characteristics in uences the transient response at a greatecarried out for cases involving both pervious and impervious pore rate. Figs. 10 and 11, respectively, illustrate the degree of consoli-pressure boundary conditions at the interface between rock socket dation for the pervious and impervious pore pressure boundaryand poroelastic medium. The numerical results presented in this conditions at the interface of the rock socket and poroelastic half paper examine both time-dependent transient translational disspace. The rate of consolidation increases where the alterations inplacement and the time-dependent degree of consolidation. The hydraulic conductivity characteristics are taken into consider- results of the computational modeling illustrate that the consideration. In addition, for the case of stress-state-dependent damagetion of hydraulic conductivity alteration during the damage evoevolution, less change has been observed. Figs. 12D21 illustrateution process has a signipcant influence on the actual timeidentical results applicable to rock socket dimensions debned bydependent translational displacement of the rock socket, whereas

0.9 Ideal poroelasticity 0.8 0.7 o (Stress-state dependent) damage 0.6 Damage (No permeability evolution) 0.5 0.4 0.3 0.2 0.1 0 10 20 30 40 50 60 \sqrt{T}

its inßuence on the degree of consolidation is marginal. This inßuence depends on the rock socket dimensions as deÞned by the length to diameter ratio. The larger this ratio, the greater the inßuence observed, and this also depends on the pore pressure boundary conditions at the interface of the rock socket and surrounding poroelastic half space. The effects are greater when the pore pressure boundary conditions correspond to an impervious interface. The dependency of the transient response on the stress state in the surrounding poroelastic half space also supports the above conclusions.

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